# Information Bottleneck for Controlling **Conciseness in Rationale Extraction**



Code <a href="https://github.com/bhargaviparanjape/explainable\_ga">https://github.com/bhargaviparanjape/explainable\_ga</a> Webpage <a href="https://bhargaviparanjape.github.io/">https://bhargaviparanjape.github.io/</a>





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# Motivation

Complex SOTA models for Text Classification, Question Answering, Fact Verification, etc. are black boxes

Query: Can pickling salt be used as table salt? **Context**: PICKLING SALT Pickling salt is a salt that is used mainly for canning and manufacturing pickles ... It can be used in place of table salt, although it can cake. A solution to this would be to add a few grains of rice to the salt .... Label: Yes **Question Answering Context:** Beware of movies with the director's name in the title. Take John Carpenter's ghosts of mars (please) ... this embarrassment would surely have bypassed theaters entirely and gone straight to its proper home on the USA network ... the latest from the director of Starman, Halloween, and Escape from New York is a lousy western all gussied up to look like a futuristic horror flick. For future generations. A matriarchal society ... Well, don't get your hopes up.

Label: Negative

### **Text Classification**

# Rationales

- Complex SOTA models are black boxes
- Tasks: Text Classification, Question Answering, Fact Verification
- Humans highlight <25% of input as evidence to explain their decision

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PICKLING SALT Pickling salt is a salt that is used mainly for canning and manufacturing pickles ... It can be used in place of table salt, although it can cake. A solution to this would be to add a few grains of rice to the salt .... Label: Yes

**Question Answering** 

### **Context:**

Beware of movies with the director's name in the title. Take John Carpenter's ghosts of mars (please) ... this embarrassment would surely have bypassed theaters entirely and gone straight to its proper home on the USA **network** ... the latest from the director of Starman, Halloween, and Escape from New York is a lousy western all gussied up to look like a futuristic horror flick. For future generations. A matriarchal society ... Well, don't get your hopes up. Label: Negative

**Text Classification** 



# Rationales

- Complex SOTA models are black boxes
- Tasks: Text Classification, Question Answering, Fact Verification
- Humans highlight <25% of input as evidence to explain their decision
- Rationale: A subsequence of input text that is necessary and sufficient for task decision
  - Sufficient Concise
  - Necessary Faithful 0

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### **Question Answering**

### **Context:**

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**Text Classification** 



# Faithfulness

The rationale must actually be used for the model's prediction.

## Query: Can pickling salt be used as table salt? **Context:**

PICKLING SALT Pickling salt is a salt that is used mainly for canning and manufacturing pickles .... It can be used in place of table salt, although it can cake. A solution to this would be to add a few grains of rice to the salt, or to bake it, and then break it apart

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# **Problem Definition**

Extract subsequence of text that is **necessary** and **sufficient** for task decision

- Sufficient (Conciseness)
- Necessary (Faithfulness)

## Outline

- Information Bottleneck Approach
- Model Architecture
- Experiments
- Results

## **Query:** Can pickling salt be used as table salt? **Context:**

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**Question Answering** 



# Faithfulness

- The rationale must be **necessary** for the model's prediction
- Faithful model design<sup>[1]</sup>:
  - Explainer identifies rationale
  - Predictor conditions only on explainer's prediction

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Model Architecture Experiments Results

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# **Accuracy-Conciseness Tradeoff**

- Explainer can makes mistakes, leading to performance loss of predictor
- Tradeoff between predictor's accuracy and rationale conciseness

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Experiments Results

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# **Accuracy-Conciseness Tradeoff**

- Explainer can makes mistakes, leading to performance loss of predictor.
- Rationale must be *optimally compressed representation* of input:
  - Conciseness: Minimally informative about the original input, and
  - 2. Accuracy: Maximally informative about the output label.

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Model Architecture Experiments

Results

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**Explainer** 



True

## Information Bottleneck (IB) Principle

Setup: A random variable X that is predictive of observed variable Y

predict **Y**.



Model Architecture Experiments Results

- **Information Bottleneck:** Find best tradeoff between accuracy and compression (conciseness)
- IB Objective: Find a compressed representation of X termed **bottleneck variable Z** that can best



## **Information Bottleneck Principle**

Υ.

Objective: **Z** should be **minimally informative** about **X** and **maximally informative** about **Y**.

Compression (Conciseness) term



I(; ) is mutual information

Model Architecture Experiments Results

## If X is predictive of Y, IB finds a compressed representation termed **bottleneck variable Z** that best predicts



## **Information Bottleneck Principle**

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Model Architecture Experiments Results

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## **Information Bottleneck Principle**

best predicts **Y**.

Objective: **Z** should be **minimally informative** about **X** and **maximally informative** about **Y**.



I(; ) is mutual information

Model Architecture Experiments Results

## If X is predictive of Y, IB aims to find a compressed representation termed **bottleneck variable Z** of that



## Variational Information Bottleneck

Model Architecture Experiments Results

## Variational lower bound on mutual information for gradient-based optimization<sup>[2]</sup>



## Variational Information Bottleneck

- Objective to minimize:
  - Task Loss: Likelihood of predicting y from z

$$L_{VIB} = \mathbb{E}_{z \sim p_{\theta}(z|x)} \left[ -\log q_{\phi} \right]$$

Task Loss Relevance (Accuracy) term Model Architecture Experiments Results

## Variational lower bound on mutual information for gradient-based optimization<sup>[2]</sup>

(y|z)]



## Variational Information Bottleneck

- Variational lower bound on mutual information for parametric optimization<sup>[2]</sup>
- Objective to minimize: lacksquare
  - Task Loss: Likelihood of predicting y from z
  - contains no information about x.

$$L_{VIB} = \mathbb{E}_{z \sim p_{\theta}(z|x)} \left[ -\log q_{\phi} \right]$$

Task Loss Relevance (Accuracy) term

Model Architecture Experiments Results

• Information Loss: Divergence between posterior p(z|x) and a prior r(z) that

 $(y|z)] + \beta KL[p_{\theta}(z|x), r(z)],$ 

Information Loss **Compression (Conciseness)** term



# Variational IB for Interpretability

- Shortcoming of the previous formulation: Bottleneck representation **z** is not interpretable as the ulletrationale!
- Our formulation: X is a sequence of words or sentences and Z is constrained to be human  $\bullet$ readable subsequence in **X**



Model Architecture Experiments Results

Masked version of the input



# Variational IB for Interpretability

- **Interpretable Information Bottleneck Formulation:** lacksquare
  - Input **x** is a sequence of words/sentences
  - Binary mask vector **m** of same size as **x** 0
  - Bottleneck z is obtained by masking x with a binary vector m 0



Model Architecture Experiments Results

Controlled Sparsity = 40% Home sapiens is the binomial nomenclature for the only extant human It is currently of least concern on the Red list of endangered species by the Rationale

m



# Variational IB for Interpretability

- **Interpretable Information Bottleneck Formulation:**  $\bullet$ 
  - Input **x** is a sequence of words/sentences
  - Binary mask vector **m** of same size as **x** 0
  - Bottleneck z is obtained by masking x with a binary vector m 0

$$L_{IVIB} = \underbrace{\mathbf{E}_{m \sim p_{\theta}(m|x)} [-\log q_{\phi}(y|m \odot x)]}_{\text{Task Loss}} + \underbrace{\mathbf{Task Loss}}_{\text{Task Loss}}$$

**Relevance (Accuracy)** term

Model Architecture Experiments Results

 $|KL[p_{\theta}(m_j|x)||r(m_j)],$ 

Information Loss Compression (Conciseness) term



# **Our Approach: Sparse IB**

$$L_{IVIB} = \underbrace{\mathbf{E}_{m \sim p_{\theta}(m|x)} [-\log q_{\phi}(y|m \odot x)]}_{\text{Task Loss}} + \underbrace{\mathbf{Task Loss}}_{\text{Task Loss}}$$

Apply knowledge of how sparse the mask should be to assign the prior over mask, r(m) a fixed value  $\pi$ 

$$L_{IVIB} = \mathbb{E}_{m \sim p_{\theta}(m|x)} [-\log q_{\phi}(y|m \odot x)] + \beta \sum_{j} \sum_{j \in \mathcal{I}_{ij}} p_{\theta}(y|m \odot x)] + \beta \sum_{j \in \mathcal{I}_{ij}} p_{\theta}(y|m \odot x) = 0$$

Model Architecture Experiments Results

 $\beta \sum KL[p_{\theta}(m_j|x)||r(m_j)],$ 

Information Loss

	Dataset	% Input as Rationale
$KL[p_{\theta}(m_j x) \parallel \pi]$	FEVER	20.0
	MultiRC	17.4
	Movies	19.1
	BoolQ	6.6
	Evidence	1.4

Table : % of input masked as rationale by humans can be used as  $\pi$ 





# **Model Architecture**

Two independent transformer-based explainer and predictor models





## **Model Architecture - Explainer**

- Input consists of a sequence of sentences  $x_1, x_2, \ldots x_i, \ldots, x_n$ lacksquare
- Explainer predicts posterior probability  $p(m_i | x)$  that  $i^{th}$  sentence is in rationale.





## **Model Architecture - Sampling**

- **Bernoulli** distribution with  $p(m_i | x)$  used to sample binary mask value  $m_i$  $\bullet$
- Gumbel softmax trick to reparameterize  $m_i$  for end-to-end differentiability  $\bullet$



Information Bottleneck Model Architecture Experiments Results

 $m \sim p(m|x)$ 



## **Model Architecture - Predictor**

while predicting task label



## Predictor/Classifier applies the sampled sentence mask over its input representation



## Experiments



Five text classification tasks from the ERASER benchmark (DeYoung et al., 2019) :

- Movies sentiment analysis •
- **FEVER** fact verification lacksquare
- MultiRC and BoolQ reading comprehension datasets ullet
- **Evidence inference** over scientific text.  $\bullet$

All these datasets have sentence-level rationale annotations for validation and test sets.

## Experiments



Five text classification tasks from the ERASER benchmark (DeYoung et al., 2019). All these datasets have sentence-level rationale annotations for validation and test sets.

## **Evaluation Metrics**

- Task Performance: Macro F1 for classification tasks
- Rationale Performance: Token-level macro F1 of predicted rationale to gold annotations  $\bullet$

## **Baseline Approaches - Sparse Norm**

- Previous work<sup>[1]</sup> minimize norm of the mask vector for conciseness.
- Value of norm is no smaller than the value of the prior  $\pi$

$$L_{IVIB} = \underbrace{\mathbf{E}_{m \sim p_{\theta}(m|x)} \left[-\log q_{\phi}(x)\right]}_{m \sim p_{\theta}(m|x)} = \underbrace{-\log q_{\phi}(x)}_{m \sim p_{\theta}(m|x)} = \underbrace{-\log q_{\phi}(m|x)}_{m \sim p_{\theta}(m|x)}_{m \sim p_{\theta}(m|x)} = \underbrace{-\log q_{\phi}(m|x)}_{m \sim p_{\theta}(m|x)} = \underbrace{-\log q_{\phi}(m|x)}_{m \sim p_{\theta}(m|$$

Task Loss

Same as the fixed prior used in information loss!



## **Baseline Approaches - No Conciseness Loss**

## Baseline that does not use the information loss term for optimization

## $L_{IVIB} = \underbrace{\mathbf{E}_{m \sim p_{\theta}(m|x)}[-\log q_{\phi}(y|m \odot x)]}_{+ \lambda \max(0, ||m|)}$

Task Loss

Norm Loss

## **Results - Task Performance**

No Conciseness Loss









## **Results - Task Performance**















## **Discussion: Controlled Sparsity**

Sparse IB (Ours)

 Achieves desired prior sparsity in expectation Information Bottleneck Model Architecture Experiments Results

$\pi$	Sparse Norm-C		Sparse IB Mean Var	
				1.24
0.25	0.11	1.14	0.26	1.67
0.40	0.38	2.90	0.42	3.02
0.20	0.04	0.84	0.22	1.91
0.20	0.10	1.17	0.20	1.61
	0.20 0.25 0.40 0.20	Mean0.200.170.250.110.400.380.200.04	MeanVar0.200.170.940.250.111.140.400.382.900.200.040.84	MeanVarMean0.200.170.940.210.250.111.140.260.400.382.900.420.200.040.840.22

Table 2: Average mask length (sparsity) attained by Sparse IB and the Sparse Norm-C baseline for a given prior  $\pi$  for different tasks, averaged over 100 runs.

## **Discussion: Controlled Sparsity**

Sparse IB (Ours)

- Achieves desired prior sparsity in expectation
- Is able to adapt to different examples

Information Bottleneck Model Architecture Experiments Results

Dataset	π	Sparse Mean	Norm-C Var	Spars Mean	e IB Var
FEVER	$0.20 \\ 0.25 \\ 0.40 \\ 0.20 \\ 0.20$	0.17	0.94	0.21	1.24
MultiRC		0.11	1.14	0.26	1.67
Movies		0.38	2.90	0.42	3.02
BoolQ		0.04	0.84	0.22	1.91
Evidence		0.10	1.17	0.20	1.61

Table 2: Average mask length (sparsity) attained by Sparse IB and the Sparse Norm-C baseline for a given prior  $\pi$  for different tasks, averaged over 100 runs.

## **Results - Task Performance**

No Conciseness Loss Sparse Norm-Controllec







Information Bottleneck Model Architecture Experiments **Results** 

Sparse IB (Us) 📕 Full Input

# **Results - Semisupervised**

- Use limited rationale supervision to close gap with a model that uses full input
- Replacing information loss term with cross-entropy term between predicted mask and human-annotated gold mask

$$L_{IVIB} = \underbrace{\mathbf{E}_{m \sim p_{\theta}(m|x)} \left[-\log q_{\phi}(y)\right]}_{\text{Task Loss}}$$

 $[m \odot x)] + \gamma \sum_{i} -\hat{m_j} \log p(m_j | x)$ Rationale Loss

# **Results - Semisupervised**

Task accuracy gap can be bridged with <50% annotations for rationales with diminishing returns as more annotated data is used



Information Bottleneck Model Architecture Experiments **Results** 



## Task Performance vs. % of Rationale Annotations **FEVER (left), MultiRC (right)**

# Conclusion

- Faithful and interpretable model using information bottleneck that jointly optimizes for conciseness of rationale and accuracy of task.
- Improvement in task and rationale performance over prior work
- Nears performance of full-input model with <50% annotation for rationales</li>

# Thank you!